## Week 2 Assignment 2

### DEY, Sankha

#### Multiple Linear Regression and Special Issues Assignment

#install.packages("GGally")  
#install.packages("MASS")  
#install.packages("car")  
#install.packages("gridExtra")  
options(tidyverse.quiet = TRUE)  
library(tidyverse)  
library(GGally)  
library(MASS)  
library(car)  
library(gridExtra)

#### Task 1

bike <- read\_csv("hour.csv")

## Parsed with column specification:  
## cols(  
## instant = col\_double(),  
## dteday = col\_date(format = ""),  
## season = col\_double(),  
## yr = col\_double(),  
## mnth = col\_double(),  
## hr = col\_double(),  
## holiday = col\_double(),  
## weekday = col\_double(),  
## workingday = col\_double(),  
## weathersit = col\_double(),  
## temp = col\_double(),  
## atemp = col\_double(),  
## hum = col\_double(),  
## windspeed = col\_double(),  
## casual = col\_double(),  
## registered = col\_double(),  
## count = col\_double()  
## )

#str(bike) # Commeneted before final knit

bike = bike %>% mutate(season = as\_factor(as.character(season))) %>%  
mutate(season = fct\_recode(season,  
"Spring" = "1",  
"Summer" = "2",  
"Fall" = "3",  
"Winter" = "4"))  
#str(bike) # Commeneted before final knit

bike = bike %>% mutate(yr = as\_factor(yr))  
bike = bike %>% mutate(mnth = as\_factor(mnth))  
bike = bike %>% mutate(hr = as\_factor(hr))  
#str(bike) # Commeneted before final knit

bike = bike %>% mutate(holiday = as\_factor(as.character(holiday))) %>%  
mutate(holiday = fct\_recode(holiday,  
"NotHoliday" = "0",  
"Holiday" = "1"))  
#str(bike) # Commeneted before final knit

bike = bike %>% mutate(workingday = as\_factor(as.character(workingday))) %>%  
mutate(workingday = fct\_recode(workingday,  
"NotWorkingDay" = "0",  
"WorkingDay" = "1"))  
#str(bike) # Commeneted before final knit

bike = bike %>% mutate(weathersit = as\_factor(as.character(weathersit))) %>%  
mutate(weathersit = fct\_recode(weathersit,  
"NoPrecip" = "1",  
"Misty" = "2",  
"LightPrecip" = "3",  
"HeavyPrecip" = "4"))  
#str(bike) # Commeneted before final knit

bike = bike %>% mutate(weekday = as\_factor(as.character(weekday))) %>%  
mutate(weekday = fct\_recode(weekday,  
"Sunday" = "0",  
"Monday" = "1",  
"Tuesday" = "2",  
"Wednesday" = "3",  
"Thursday" = "4",  
"Friday" = "5",  
"Saturday" = "6"))  
str(bike)

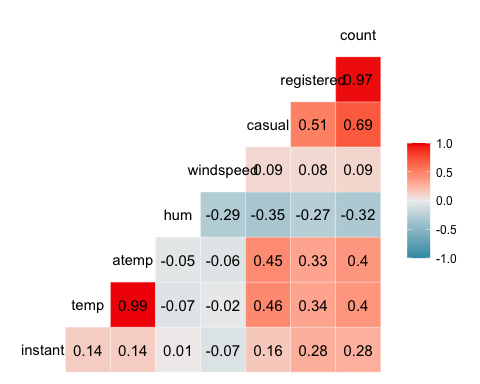
## Classes 'spec\_tbl\_df', 'tbl\_df', 'tbl' and 'data.frame': 17379 obs. of 17 variables:  
## $ instant : num 1 2 3 4 5 6 7 8 9 10 ...  
## $ dteday : Date, format: "2011-01-01" "2011-01-01" ...  
## $ season : Factor w/ 4 levels "Spring","Summer",..: 1 1 1 1 1 1 1 1 1 1 ...  
## $ yr : Factor w/ 2 levels "0","1": 1 1 1 1 1 1 1 1 1 1 ...  
## $ mnth : Factor w/ 12 levels "1","2","3","4",..: 1 1 1 1 1 1 1 1 1 1 ...  
## $ hr : Factor w/ 24 levels "0","1","2","3",..: 1 2 3 4 5 6 7 8 9 10 ...  
## $ holiday : Factor w/ 2 levels "NotHoliday","Holiday": 1 1 1 1 1 1 1 1 1 1 ...  
## $ weekday : Factor w/ 7 levels "Saturday","Sunday",..: 1 1 1 1 1 1 1 1 1 1 ...  
## $ workingday: Factor w/ 2 levels "NotWorkingDay",..: 1 1 1 1 1 1 1 1 1 1 ...  
## $ weathersit: Factor w/ 4 levels "NoPrecip","Misty",..: 1 1 1 1 1 2 1 1 1 1 ...  
## $ temp : num 0.24 0.22 0.22 0.24 0.24 0.24 0.22 0.2 0.24 0.32 ...  
## $ atemp : num 0.288 0.273 0.273 0.288 0.288 ...  
## $ hum : num 0.81 0.8 0.8 0.75 0.75 0.75 0.8 0.86 0.75 0.76 ...  
## $ windspeed : num 0 0 0 0 0 0.0896 0 0 0 0 ...  
## $ casual : num 3 8 5 3 0 0 2 1 1 8 ...  
## $ registered: num 13 32 27 10 1 1 0 2 7 6 ...  
## $ count : num 16 40 32 13 1 1 2 3 8 14 ...

Though these variables (“yr”, “mnth”, and “hr”) represent numeric data, they are kind of cyclic variable and not considered in correlation matrix and ggcorr function. We dont want their usability as continoious variables. Like hr value with 23 is not greater than hr value 1. They just represent two different timespans. These variables actually represent factor values with separate, independent coefficient (or more precisely, degree of freedom) for each hour of the day or each month of the year.

#### Task 2

ggcorr(bike, label = "TRUE", label\_round = 2)

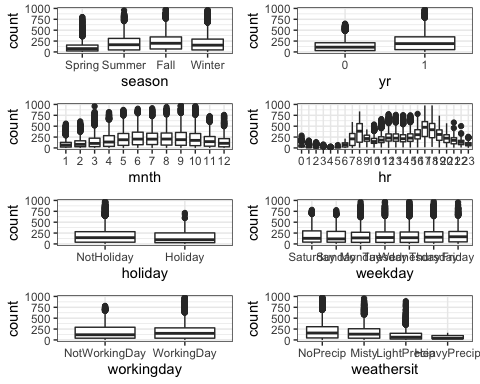
## Warning in ggcorr(bike, label = "TRUE", label\_round = 2): data in column(s)  
## 'dteday', 'season', 'yr', 'mnth', 'hr', 'holiday', 'weekday', 'workingday',  
## 'weathersit' are not numeric and were ignored



temp and atemp have the higher correlation with count with a correlation value of 0.4. both these two variables (temp and atemp) are strongly correlated to each other (0.99).

#### Task 3

p1 = ggplot(bike, aes(x=season,y=count)) + geom\_boxplot() + theme\_bw()  
p2 = ggplot(bike, aes(x=yr,y=count)) + geom\_boxplot() + theme\_bw()  
p3 = ggplot(bike, aes(x=mnth,y=count)) + geom\_boxplot() + theme\_bw()  
p4 = ggplot(bike, aes(x=hr,y=count)) + geom\_boxplot() + theme\_bw()  
p5 = ggplot(bike, aes(x=holiday,y=count)) + geom\_boxplot() + theme\_bw()  
p6 = ggplot(bike, aes(x=weekday,y=count)) + geom\_boxplot() + theme\_bw()  
p7 = ggplot(bike, aes(x=workingday,y=count)) + geom\_boxplot() + theme\_bw()  
p8 = ggplot(bike, aes(x=weathersit,y=count)) + geom\_boxplot() + theme\_bw()  
grid.arrange(p1,p2,p3,p4,p5,p6,p7,p8, ncol = 2)



The variable hr appears to affect count. The corresponding boxplot has a good fluctuations on count over different hours of the day. Hours 0 to 6 have almost negligible count where as hours between 7 and 8 and 17 to 19, we see a spike.  
Season - It has a moderate to low impact on count. Bike share counts are higher during summer and fall with more sunlight.  
yr - though counts are higher in 2012, there are not much overall impact. Count depends on temp and hr. mnth - Don’t have much impact on count. Bike sharing count is high at summer and fall months with more daylights and sunny days.  
hr - This one has most impact on count. It’s obvious that during the day time people will do bike sharing more. holiday - No impact. Bike sharing doesnt depend on whether its a holiday or not. Deciding creteria on temp, weather on that day. weekday - same as holiday. no impact on count. workingday - no impact. same as holiday. Not much Impact. Depends on Temp, Hour and weather. weathesit - somewhat impacts on count. Clear sunny days have more counts thant rainy days. this is also obvious.

#### Task 4

bike1 = bike %>% dplyr::select(-c(instant, dteday, registered, casual))

Creating Empty Model

emptymod = lm(count ~1, bike1) #use ~1 to build an empty model  
summary(emptymod)

##   
## Call:  
## lm(formula = count ~ 1, data = bike1)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -188.46 -149.46 -47.46 91.54 787.54   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) 189.463 1.376 137.7 <2e-16 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 181.4 on 17378 degrees of freedom

allmod = lm(count ~., bike1) #use the ~. to include all predictors rather than typing them all in  
summary(allmod)

##   
## Call:  
## lm(formula = count ~ ., data = bike1)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -393.87 -60.66 -7.96 51.31 439.18   
##   
## Coefficients: (1 not defined because of singularities)  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) -67.542 6.612 -10.216 < 2e-16 \*\*\*  
## seasonSummer 38.178 4.856 7.862 4.00e-15 \*\*\*  
## seasonFall 32.055 5.749 5.575 2.51e-08 \*\*\*  
## seasonWinter 67.994 4.882 13.928 < 2e-16 \*\*\*  
## yr1 85.431 1.563 54.658 < 2e-16 \*\*\*  
## mnth2 3.426 3.920 0.874 0.38219   
## mnth3 14.299 4.407 3.244 0.00118 \*\*   
## mnth4 6.230 6.548 0.951 0.34144   
## mnth5 20.657 7.007 2.948 0.00320 \*\*   
## mnth6 6.238 7.205 0.866 0.38662   
## mnth7 -13.269 8.082 -1.642 0.10065   
## mnth8 7.897 7.879 1.002 0.31622   
## mnth9 32.269 7.001 4.609 4.07e-06 \*\*\*  
## mnth10 15.843 6.483 2.444 0.01455 \*   
## mnth11 -9.840 6.238 -1.577 0.11474   
## mnth12 -6.256 4.954 -1.263 0.20672   
## hr1 -17.294 5.345 -3.236 0.00122 \*\*   
## hr2 -26.369 5.364 -4.916 8.91e-07 \*\*\*  
## hr3 -37.112 5.403 -6.869 6.67e-12 \*\*\*  
## hr4 -40.263 5.408 -7.445 1.01e-13 \*\*\*  
## hr5 -23.501 5.373 -4.374 1.23e-05 \*\*\*  
## hr6 35.393 5.359 6.605 4.10e-11 \*\*\*  
## hr7 170.418 5.348 31.864 < 2e-16 \*\*\*  
## hr8 310.801 5.342 58.183 < 2e-16 \*\*\*  
## hr9 163.101 5.347 30.501 < 2e-16 \*\*\*  
## hr10 108.444 5.370 20.196 < 2e-16 \*\*\*  
## hr11 133.843 5.409 24.742 < 2e-16 \*\*\*  
## hr12 173.142 5.456 31.735 < 2e-16 \*\*\*  
## hr13 168.102 5.494 30.600 < 2e-16 \*\*\*  
## hr14 152.249 5.525 27.558 < 2e-16 \*\*\*  
## hr15 161.707 5.535 29.213 < 2e-16 \*\*\*  
## hr16 223.834 5.524 40.522 < 2e-16 \*\*\*  
## hr17 377.535 5.491 68.750 < 2e-16 \*\*\*  
## hr18 345.587 5.455 63.350 < 2e-16 \*\*\*  
## hr19 236.919 5.404 43.841 < 2e-16 \*\*\*  
## hr20 157.293 5.375 29.266 < 2e-16 \*\*\*  
## hr21 107.840 5.353 20.147 < 2e-16 \*\*\*  
## hr22 70.907 5.343 13.272 < 2e-16 \*\*\*  
## hr23 32.112 5.338 6.015 1.83e-09 \*\*\*  
## holidayHoliday -26.228 4.881 -5.374 7.81e-08 \*\*\*  
## weekdaySunday -16.089 2.878 -5.591 2.30e-08 \*\*\*  
## weekdayMonday -6.814 2.970 -2.294 0.02180 \*   
## weekdayTuesday -5.240 2.899 -1.807 0.07071 .   
## weekdayWednesday -2.464 2.894 -0.851 0.39469   
## weekdayThursday -2.940 2.892 -1.016 0.30947   
## weekdayFriday 1.356 2.885 0.470 0.63823   
## workingdayWorkingDay NA NA NA NA   
## weathersitMisty -10.409 1.920 -5.421 6.00e-08 \*\*\*  
## weathersitLightPrecip -65.189 3.236 -20.145 < 2e-16 \*\*\*  
## weathersitHeavyPrecip -62.580 58.893 -1.063 0.28797   
## temp 116.384 29.513 3.943 8.06e-05 \*\*\*  
## atemp 127.975 30.624 4.179 2.94e-05 \*\*\*  
## hum -82.802 5.554 -14.909 < 2e-16 \*\*\*  
## windspeed -29.167 7.052 -4.136 3.55e-05 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 101.7 on 17326 degrees of freedom  
## Multiple R-squared: 0.6864, Adjusted R-squared: 0.6854   
## F-statistic: 729.1 on 52 and 17326 DF, p-value: < 2.2e-16

Forward stepwise regression

forwardmod = stepAIC(emptymod, direction = "forward", scope=list(upper=allmod,lower=emptymod), trace = TRUE)

## Start: AIC=180764.7  
## count ~ 1  
##   
## Df Sum of Sq RSS AIC  
## + hr 23 286734681 285026910 168713  
## + temp 1 93677759 478083832 177657  
## + atemp 1 91907421 479854170 177721  
## + hum 1 59618351 512143240 178853  
## + mnth 11 42909976 528851615 179431  
## + season 3 37729358 534032233 179584  
## + yr 1 35876722 535884870 179641  
## + weathersit 3 12285030 559476561 180393  
## + windspeed 1 4970060 566791531 180615  
## + holiday 1 546889 571214702 180750  
## + workingday 1 524387 571237204 180751  
## + weekday 6 687929 571073662 180756  
## <none> 571761591 180765  
##   
## Step: AIC=168712.5  
## count ~ hr  
##   
## Df Sum of Sq RSS AIC  
## + atemp 1 50518941 234507969 165324  
## + temp 1 50101685 234925225 165355  
## + mnth 11 44822160 240204750 165761  
## + season 3 39619754 245407156 166117  
## + yr 1 36875130 248151780 166307  
## + weathersit 3 13766672 271260238 167858  
## + hum 1 4924310 280102600 168412  
## + windspeed 1 1476211 283550699 168624  
## + holiday 1 561784 284465126 168680  
## + weekday 6 719530 284307380 168681  
## + workingday 1 485366 284541544 168685  
## <none> 285026910 168713  
##   
## Step: AIC=165324  
## count ~ hr + atemp  
##   
## Df Sum of Sq RSS AIC  
## + yr 1 33463769 201044200 162650  
## + weathersit 3 9227265 225280704 164632  
## + hum 1 7008684 227499285 164799  
## + season 3 6580442 227927527 164835  
## + mnth 11 5854560 228653409 164907  
## + weekday 6 607638 233900331 165291  
## + holiday 1 274006 234233963 165306  
## + temp 1 152153 234355816 165315  
## + windspeed 1 120557 234387412 165317  
## + workingday 1 90170 234417799 165319  
## <none> 234507969 165324  
##   
## Step: AIC=162650.2  
## count ~ hr + atemp + yr  
##   
## Df Sum of Sq RSS AIC  
## + weathersit 3 8408358 192635842 161914  
## + season 3 7190305 193853896 162023  
## + mnth 11 6486062 194558138 162102  
## + hum 1 4341837 196702363 162273  
## + weekday 6 641648 200402552 162607  
## + holiday 1 324763 200719438 162624  
## + windspeed 1 109311 200934889 162643  
## + workingday 1 106404 200937797 162643  
## + temp 1 91735 200952465 162644  
## <none> 201044200 162650  
##   
## Step: AIC=161913.7  
## count ~ hr + atemp + yr + weathersit  
##   
## Df Sum of Sq RSS AIC  
## + season 3 7771024 184864818 161204  
## + mnth 11 7464989 185170852 161249  
## + hum 1 805099 191830743 161843  
## + weekday 6 686172 191949670 161864  
## + holiday 1 413536 192222305 161878  
## + workingday 1 212428 192423414 161897  
## + temp 1 134482 192501360 161904  
## + windspeed 1 44407 192591435 161912  
## <none> 192635842 161914  
##   
## Step: AIC=161204.1  
## count ~ hr + atemp + yr + weathersit + season  
##   
## Df Sum of Sq RSS AIC  
## + mnth 11 2051323 182813495 161032  
## + hum 1 1810161 183054657 161035  
## + weekday 6 704303 184160515 161150  
## + holiday 1 392702 184472116 161169  
## + temp 1 352584 184512234 161173  
## + workingday 1 214973 184649845 161186  
## <none> 184864818 161204  
## + windspeed 1 158 184864660 161206  
##   
## Step: AIC=161032.2  
## count ~ hr + atemp + yr + weathersit + season + mnth  
##   
## Df Sum of Sq RSS AIC  
## + hum 1 2356411 180457084 160809  
## + weekday 6 692672 182120823 160978  
## + holiday 1 312321 182501174 161004  
## + temp 1 233052 182580443 161012  
## + workingday 1 203953 182609542 161015  
## <none> 182813495 161032  
## + windspeed 1 68 182813428 161034  
##   
## Step: AIC=160808.7  
## count ~ hr + atemp + yr + weathersit + season + mnth + hum  
##   
## Df Sum of Sq RSS AIC  
## + weekday 6 581105 179875980 160765  
## + holiday 1 322997 180134087 160780  
## + workingday 1 194139 180262945 160792  
## + windspeed 1 114287 180342797 160800  
## + temp 1 100025 180357059 160801  
## <none> 180457084 160809  
##   
## Step: AIC=160764.7  
## count ~ hr + atemp + yr + weathersit + season + mnth + hum +   
## weekday  
##   
## Df Sum of Sq RSS AIC  
## + holiday 1 274717 179601263 160740  
## + workingday 1 274717 179601263 160740  
## + windspeed 1 112085 179763895 160756  
## + temp 1 77171 179798809 160759  
## <none> 179875980 160765  
##   
## Step: AIC=160740.1  
## count ~ hr + atemp + yr + weathersit + season + mnth + hum +   
## weekday + holiday  
##   
## Df Sum of Sq RSS AIC  
## + windspeed 1 111562 179489701 160731  
## + temp 1 95460 179505803 160733  
## <none> 179601263 160740  
##   
## Step: AIC=160731.3  
## count ~ hr + atemp + yr + weathersit + season + mnth + hum +   
## weekday + holiday + windspeed  
##   
## Df Sum of Sq RSS AIC  
## + temp 1 160954 179328746 160718  
## <none> 179489701 160731  
##   
## Step: AIC=160717.7  
## count ~ hr + atemp + yr + weathersit + season + mnth + hum +   
## weekday + holiday + windspeed + temp  
##   
## Df Sum of Sq RSS AIC  
## <none> 179328746 160718

summary(forwardmod)

##   
## Call:  
## lm(formula = count ~ hr + atemp + yr + weathersit + season +   
## mnth + hum + weekday + holiday + windspeed + temp, data = bike1)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -393.87 -60.66 -7.96 51.31 439.18   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) -67.542 6.612 -10.216 < 2e-16 \*\*\*  
## hr1 -17.294 5.345 -3.236 0.00122 \*\*   
## hr2 -26.369 5.364 -4.916 8.91e-07 \*\*\*  
## hr3 -37.112 5.403 -6.869 6.67e-12 \*\*\*  
## hr4 -40.263 5.408 -7.445 1.01e-13 \*\*\*  
## hr5 -23.501 5.373 -4.374 1.23e-05 \*\*\*  
## hr6 35.393 5.359 6.605 4.10e-11 \*\*\*  
## hr7 170.418 5.348 31.864 < 2e-16 \*\*\*  
## hr8 310.801 5.342 58.183 < 2e-16 \*\*\*  
## hr9 163.101 5.347 30.501 < 2e-16 \*\*\*  
## hr10 108.444 5.370 20.196 < 2e-16 \*\*\*  
## hr11 133.843 5.409 24.742 < 2e-16 \*\*\*  
## hr12 173.142 5.456 31.735 < 2e-16 \*\*\*  
## hr13 168.102 5.494 30.600 < 2e-16 \*\*\*  
## hr14 152.249 5.525 27.558 < 2e-16 \*\*\*  
## hr15 161.707 5.535 29.213 < 2e-16 \*\*\*  
## hr16 223.834 5.524 40.522 < 2e-16 \*\*\*  
## hr17 377.535 5.491 68.750 < 2e-16 \*\*\*  
## hr18 345.587 5.455 63.350 < 2e-16 \*\*\*  
## hr19 236.919 5.404 43.841 < 2e-16 \*\*\*  
## hr20 157.293 5.375 29.266 < 2e-16 \*\*\*  
## hr21 107.840 5.353 20.147 < 2e-16 \*\*\*  
## hr22 70.907 5.343 13.272 < 2e-16 \*\*\*  
## hr23 32.112 5.338 6.015 1.83e-09 \*\*\*  
## atemp 127.975 30.624 4.179 2.94e-05 \*\*\*  
## yr1 85.431 1.563 54.658 < 2e-16 \*\*\*  
## weathersitMisty -10.409 1.920 -5.421 6.00e-08 \*\*\*  
## weathersitLightPrecip -65.189 3.236 -20.145 < 2e-16 \*\*\*  
## weathersitHeavyPrecip -62.580 58.893 -1.063 0.28797   
## seasonSummer 38.178 4.856 7.862 4.00e-15 \*\*\*  
## seasonFall 32.055 5.749 5.575 2.51e-08 \*\*\*  
## seasonWinter 67.994 4.882 13.928 < 2e-16 \*\*\*  
## mnth2 3.426 3.920 0.874 0.38219   
## mnth3 14.299 4.407 3.244 0.00118 \*\*   
## mnth4 6.230 6.548 0.951 0.34144   
## mnth5 20.657 7.007 2.948 0.00320 \*\*   
## mnth6 6.238 7.205 0.866 0.38662   
## mnth7 -13.269 8.082 -1.642 0.10065   
## mnth8 7.897 7.879 1.002 0.31622   
## mnth9 32.269 7.001 4.609 4.07e-06 \*\*\*  
## mnth10 15.843 6.483 2.444 0.01455 \*   
## mnth11 -9.840 6.238 -1.577 0.11474   
## mnth12 -6.256 4.954 -1.263 0.20672   
## hum -82.802 5.554 -14.909 < 2e-16 \*\*\*  
## weekdaySunday -16.089 2.878 -5.591 2.30e-08 \*\*\*  
## weekdayMonday -6.814 2.970 -2.294 0.02180 \*   
## weekdayTuesday -5.240 2.899 -1.807 0.07071 .   
## weekdayWednesday -2.464 2.894 -0.851 0.39469   
## weekdayThursday -2.940 2.892 -1.016 0.30947   
## weekdayFriday 1.356 2.885 0.470 0.63823   
## holidayHoliday -26.228 4.881 -5.374 7.81e-08 \*\*\*  
## windspeed -29.167 7.052 -4.136 3.55e-05 \*\*\*  
## temp 116.384 29.513 3.943 8.06e-05 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 101.7 on 17326 degrees of freedom  
## Multiple R-squared: 0.6864, Adjusted R-squared: 0.6854   
## F-statistic: 729.1 on 52 and 17326 DF, p-value: < 2.2e-16

Following variables are included in the forward model - hr + atemp + yr + weathersit + season + mnth + hum + weekday + holiday + windspeed + temp.  
Overall quality of the model is good with R-squared value is 0.685 and all variables (some dummy variables in cases) have p-values less than 0.05.  
This model also matches with our intuition for most of the variables except season and mnth. The slope of SeasonWinter is greater than the same of SeasonSummer or SeasonFall. This is kind of odd. Similarly slope of mnth7 became negative which ideally should be positive.

vif(forwardmod)

## GVIF Df GVIF^(1/(2\*Df))  
## hr 1.749392 23 1.012232  
## atemp 46.501555 1 6.819205  
## yr 1.025491 1 1.012665  
## weathersit 1.394544 3 1.056993  
## season 164.047934 3 2.339709  
## mnth 320.419121 11 1.299859  
## hum 1.927632 1 1.388392  
## weekday 1.129157 6 1.010174  
## holiday 1.117660 1 1.057195  
## windspeed 1.249705 1 1.117902  
## temp 54.224994 1 7.363762

With above vif model, temp and atemp have GVIF^(1/(2\*Df)) value greater than 5. So these two variables can be considered for multicollinearity.

#### Task 5:

backmod = stepAIC(allmod, direction = "backward", trace = TRUE)

## Start: AIC=160717.7  
## count ~ season + yr + mnth + hr + holiday + weekday + workingday +   
## weathersit + temp + atemp + hum + windspeed  
##   
##   
## Step: AIC=160717.7  
## count ~ season + yr + mnth + hr + holiday + weekday + weathersit +   
## temp + atemp + hum + windspeed  
##   
## Df Sum of Sq RSS AIC  
## <none> 179328746 160718  
## - temp 1 160954 179489701 160731  
## - windspeed 1 177057 179505803 160733  
## - atemp 1 180751 179509498 160733  
## - holiday 1 298893 179627639 160745  
## - weekday 6 498795 179827541 160754  
## - mnth 11 2426171 181754917 160929  
## - hum 1 2300667 181629413 160937  
## - season 3 2398467 181727213 160943  
## - weathersit 3 4208731 183537478 161115  
## - yr 1 30920851 210249597 163480  
## - hr 23 196741474 376070220 173542

summary(backmod)

##   
## Call:  
## lm(formula = count ~ season + yr + mnth + hr + holiday + weekday +   
## weathersit + temp + atemp + hum + windspeed, data = bike1)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -393.87 -60.66 -7.96 51.31 439.18   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) -67.542 6.612 -10.216 < 2e-16 \*\*\*  
## seasonSummer 38.178 4.856 7.862 4.00e-15 \*\*\*  
## seasonFall 32.055 5.749 5.575 2.51e-08 \*\*\*  
## seasonWinter 67.994 4.882 13.928 < 2e-16 \*\*\*  
## yr1 85.431 1.563 54.658 < 2e-16 \*\*\*  
## mnth2 3.426 3.920 0.874 0.38219   
## mnth3 14.299 4.407 3.244 0.00118 \*\*   
## mnth4 6.230 6.548 0.951 0.34144   
## mnth5 20.657 7.007 2.948 0.00320 \*\*   
## mnth6 6.238 7.205 0.866 0.38662   
## mnth7 -13.269 8.082 -1.642 0.10065   
## mnth8 7.897 7.879 1.002 0.31622   
## mnth9 32.269 7.001 4.609 4.07e-06 \*\*\*  
## mnth10 15.843 6.483 2.444 0.01455 \*   
## mnth11 -9.840 6.238 -1.577 0.11474   
## mnth12 -6.256 4.954 -1.263 0.20672   
## hr1 -17.294 5.345 -3.236 0.00122 \*\*   
## hr2 -26.369 5.364 -4.916 8.91e-07 \*\*\*  
## hr3 -37.112 5.403 -6.869 6.67e-12 \*\*\*  
## hr4 -40.263 5.408 -7.445 1.01e-13 \*\*\*  
## hr5 -23.501 5.373 -4.374 1.23e-05 \*\*\*  
## hr6 35.393 5.359 6.605 4.10e-11 \*\*\*  
## hr7 170.418 5.348 31.864 < 2e-16 \*\*\*  
## hr8 310.801 5.342 58.183 < 2e-16 \*\*\*  
## hr9 163.101 5.347 30.501 < 2e-16 \*\*\*  
## hr10 108.444 5.370 20.196 < 2e-16 \*\*\*  
## hr11 133.843 5.409 24.742 < 2e-16 \*\*\*  
## hr12 173.142 5.456 31.735 < 2e-16 \*\*\*  
## hr13 168.102 5.494 30.600 < 2e-16 \*\*\*  
## hr14 152.249 5.525 27.558 < 2e-16 \*\*\*  
## hr15 161.707 5.535 29.213 < 2e-16 \*\*\*  
## hr16 223.834 5.524 40.522 < 2e-16 \*\*\*  
## hr17 377.535 5.491 68.750 < 2e-16 \*\*\*  
## hr18 345.587 5.455 63.350 < 2e-16 \*\*\*  
## hr19 236.919 5.404 43.841 < 2e-16 \*\*\*  
## hr20 157.293 5.375 29.266 < 2e-16 \*\*\*  
## hr21 107.840 5.353 20.147 < 2e-16 \*\*\*  
## hr22 70.907 5.343 13.272 < 2e-16 \*\*\*  
## hr23 32.112 5.338 6.015 1.83e-09 \*\*\*  
## holidayHoliday -26.228 4.881 -5.374 7.81e-08 \*\*\*  
## weekdaySunday -16.089 2.878 -5.591 2.30e-08 \*\*\*  
## weekdayMonday -6.814 2.970 -2.294 0.02180 \*   
## weekdayTuesday -5.240 2.899 -1.807 0.07071 .   
## weekdayWednesday -2.464 2.894 -0.851 0.39469   
## weekdayThursday -2.940 2.892 -1.016 0.30947   
## weekdayFriday 1.356 2.885 0.470 0.63823   
## weathersitMisty -10.409 1.920 -5.421 6.00e-08 \*\*\*  
## weathersitLightPrecip -65.189 3.236 -20.145 < 2e-16 \*\*\*  
## weathersitHeavyPrecip -62.580 58.893 -1.063 0.28797   
## temp 116.384 29.513 3.943 8.06e-05 \*\*\*  
## atemp 127.975 30.624 4.179 2.94e-05 \*\*\*  
## hum -82.802 5.554 -14.909 < 2e-16 \*\*\*  
## windspeed -29.167 7.052 -4.136 3.55e-05 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 101.7 on 17326 degrees of freedom  
## Multiple R-squared: 0.6864, Adjusted R-squared: 0.6854   
## F-statistic: 729.1 on 52 and 17326 DF, p-value: < 2.2e-16

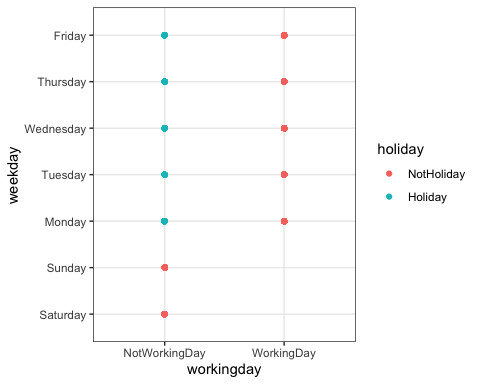
vif(backmod)

## GVIF Df GVIF^(1/(2\*Df))  
## season 164.047934 3 2.339709  
## yr 1.025491 1 1.012665  
## mnth 320.419121 11 1.299859  
## hr 1.749392 23 1.012232  
## holiday 1.117660 1 1.057195  
## weekday 1.129157 6 1.010174  
## weathersit 1.394544 3 1.056993  
## temp 54.224994 1 7.363762  
## atemp 46.501555 1 6.819205  
## hum 1.927632 1 1.388392  
## windspeed 1.249705 1 1.117902

Both models are looking same with R-Squared value - 0.685 and AIC - 160718 and RSS 179328746. Both models show temp and atemp have higher GVIF^(1/(2\*Df)) value, greater than 5. So these two variables can be considered for multicollinearity. No differentiation noted between two models.

#### Task 6

#ggpairs(bike, columns = c(7:17))  
ggplot(bike1,aes(x=workingday,y=weekday,color=holiday)) + geom\_point() + theme\_bw()

 workingday is presented by weekday and holiday and kicked out by these two variables.

#### Task 7

We have not considered variable interactions in this model and didnt take care the interaction effects. Interaction terms are introduced to account for different effects when two independent variables combine in some interesting way. There are a few categorial variables that we had in our model. So, variabe interaction term is missing in our model.